

# Exercises: Artificial Intelligence

A\*

A\*

# A\* ALGORITHM

# A\* Algorithm

- ***Input:***

- **QUEUE:** Path only containing root

- ***Algorithm:***

- **WHILE** (QUEUE not empty && first path not reach goal) **DO**

- Remove ***first path*** from QUEUE

- Create paths to all children

- Reject paths with loops

- Add paths and sort QUEUE (by  $f = \text{cost} + \text{heuristic}$ )

- **IF** QUEUE contains paths: P, Q

- AND** P ends in node  $N_i$  && Q contains node  $N_i$

- AND** cost P  $\geq$  cost Q

- THEN** remove P

- **IF** goal reached **THEN** success **ELSE** failure

A\*

**FIRST EXAMPLE ON A\***

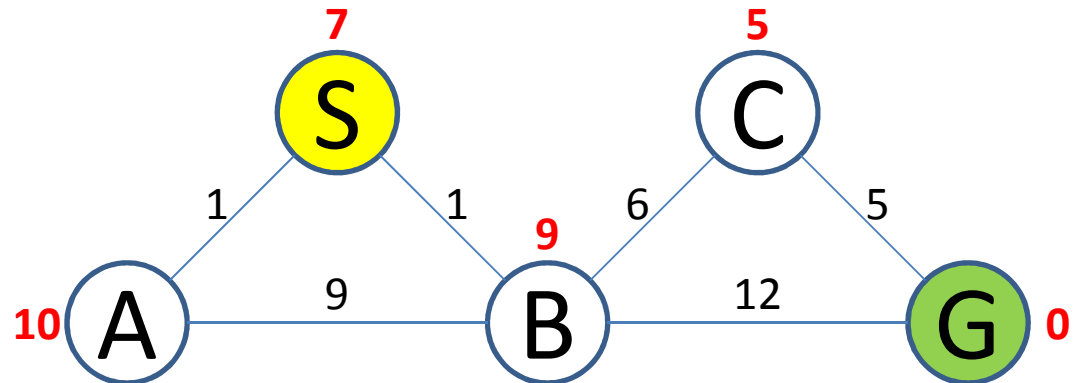
# A\* algorithm by Example



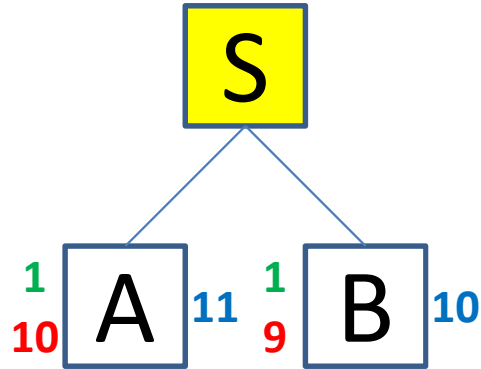
$f = \text{accumulated path cost} + \text{heuristic}$

QUEUE = *path containing root*

QUEUE: <S>



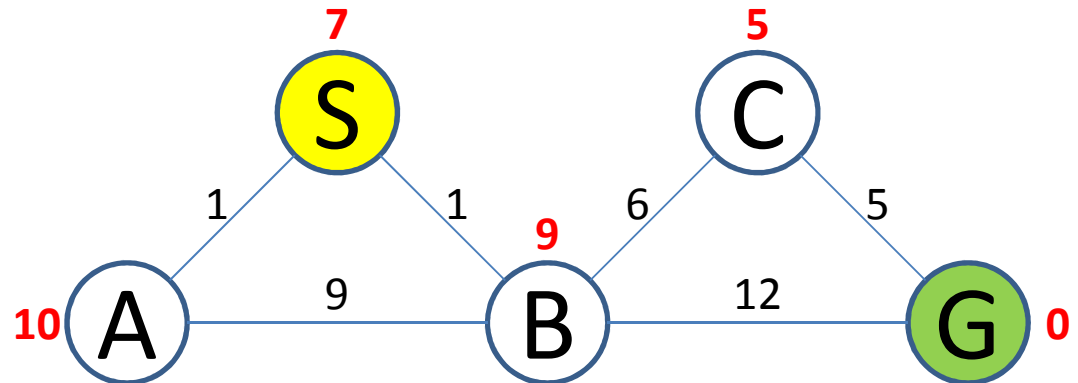
# A\* algorithm by Example



$f = \text{accumulated path cost} + \text{heuristic}$

Remove ***first path***, Create ***paths to all children***, Reject ***loops*** and ***Add paths***.  
***Sort QUEUE by f***

**QUEUE: <SB,SA>**

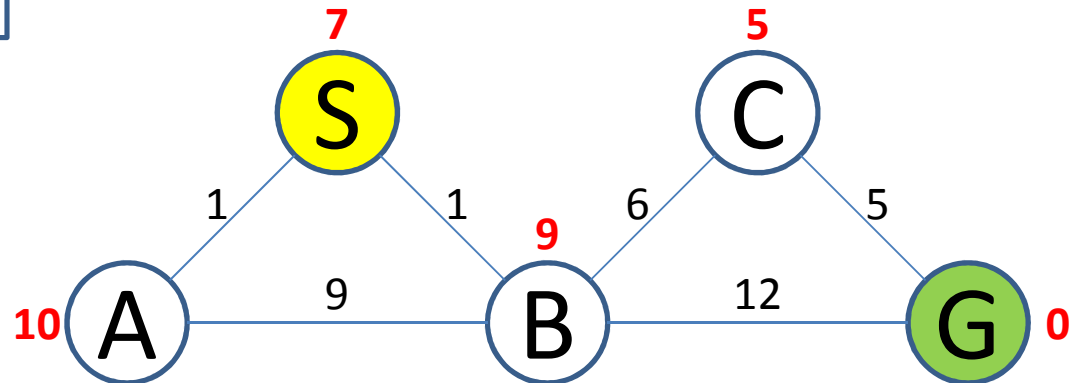
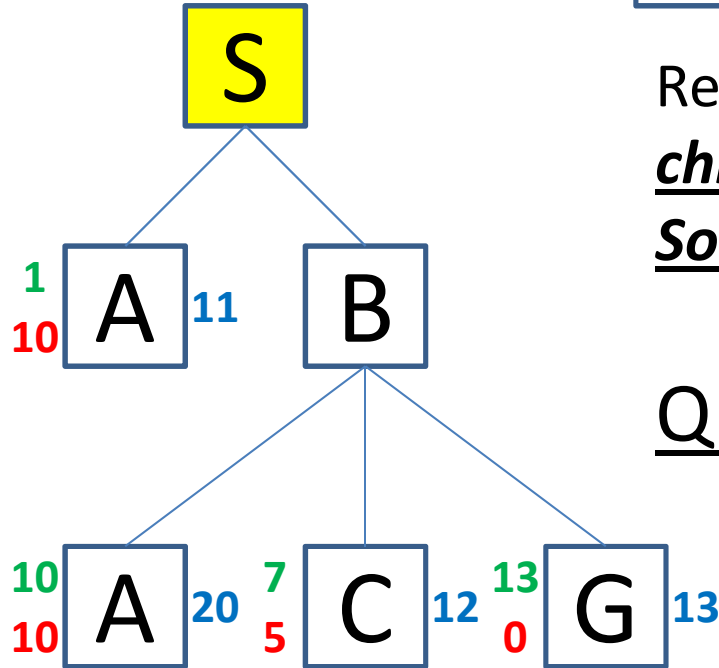


# A\* algorithm by Example

$$f = \text{accumulated path cost} + \text{heuristic}$$

Remove ***first path***, Create ***paths to all children***, Reject ***loops*** and ***Add paths***.  
***Sort QUEUE by f***

**QUEUE**: <SA,SBC,SBG,SBA>

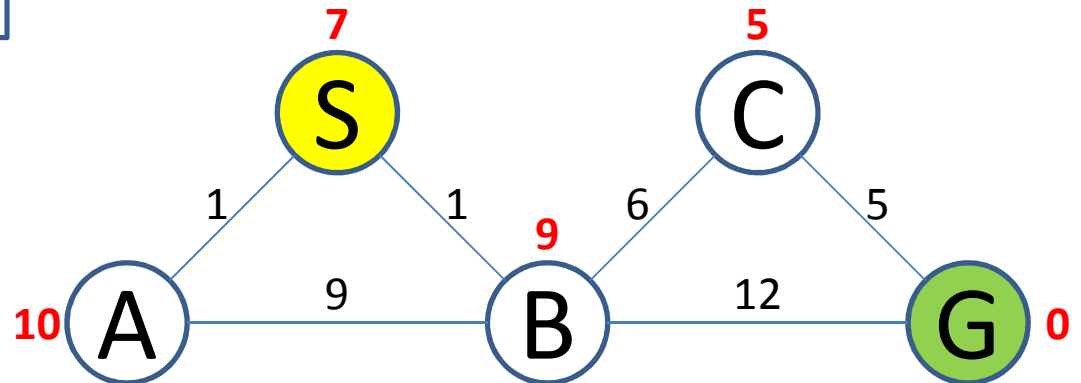
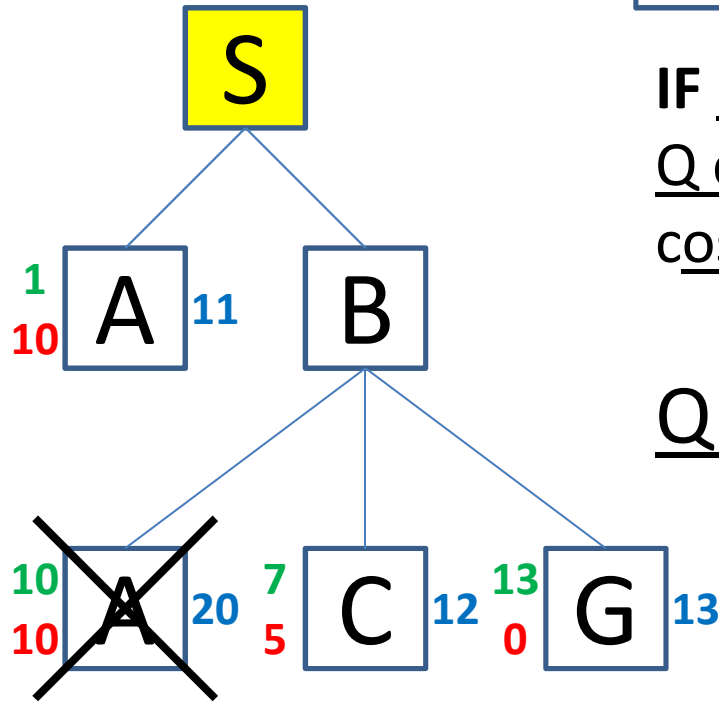


# A\* algorithm by Example

$f = \text{accumulated path cost} + \text{heuristic}$

IF P terminating in I with cost P &&  
Q containing I with cost Q **AND**  
cost P  $\geq$  cost Q **THEN** remove P

QUEUE: <SA, SBC, SBG, SBA>



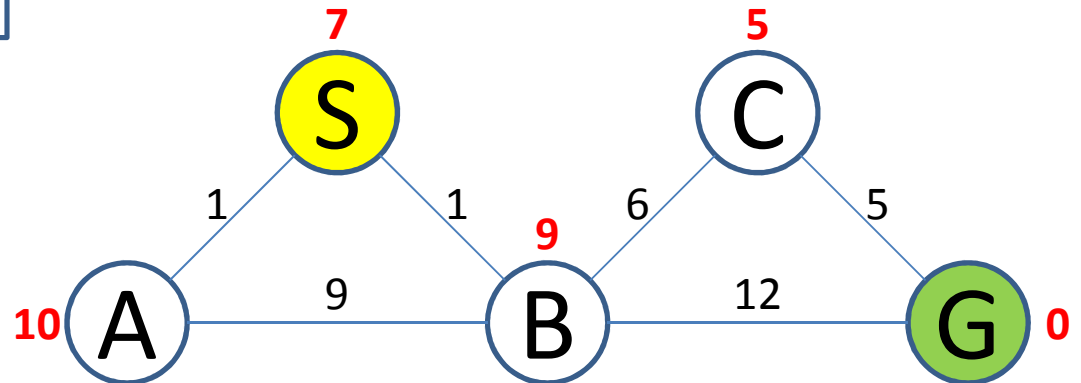
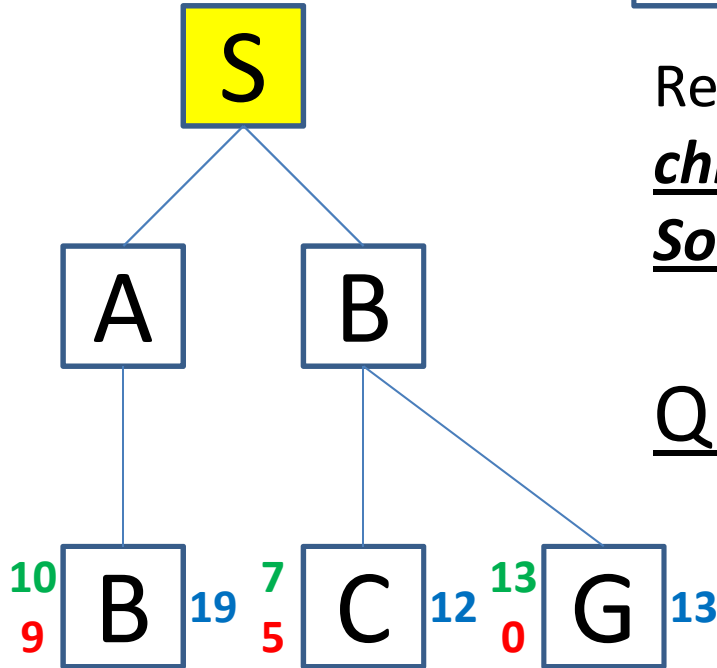


# A\* algorithm by Example

$f = \text{accumulated path cost} + \text{heuristic}$

Remove ***first path***, Create ***paths to all children***, Reject ***loops*** and ***Add paths***.  
***Sort QUEUE by f***

***QUEUE: <SBC,SBG,SAB>***

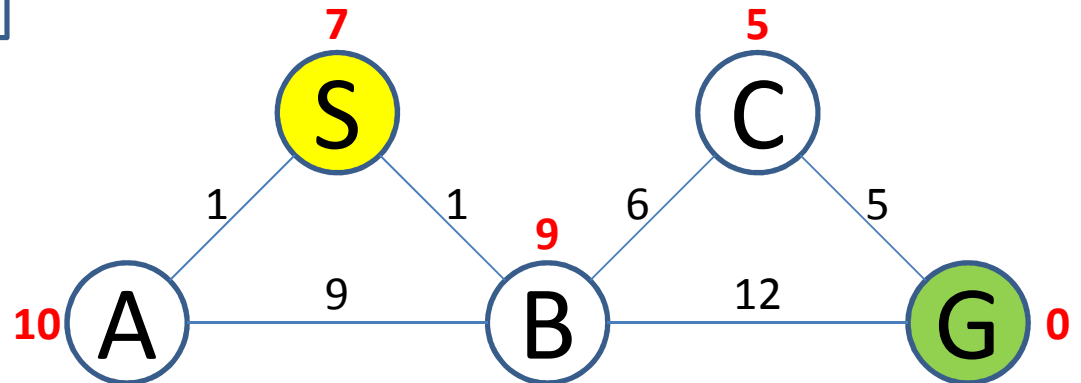
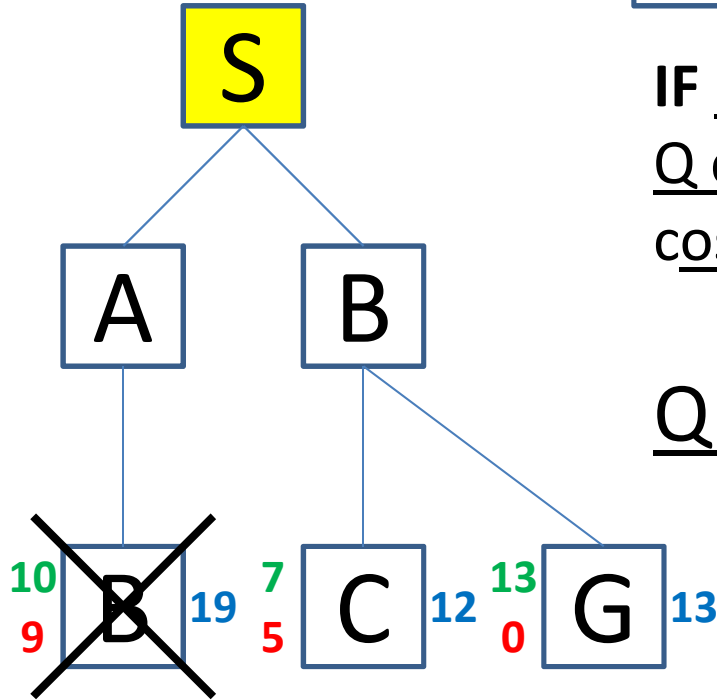


# A\* algorithm by Example

$f = \text{accumulated path cost} + \text{heuristic}$

IF P terminating in I with cost P &&  
Q containing I with cost Q **AND**  
cost P  $\geq$  cost Q **THEN** remove P

QUEUE:  $\langle \text{SBC}, \text{SBG}, \underline{\text{SAB}} \rangle$

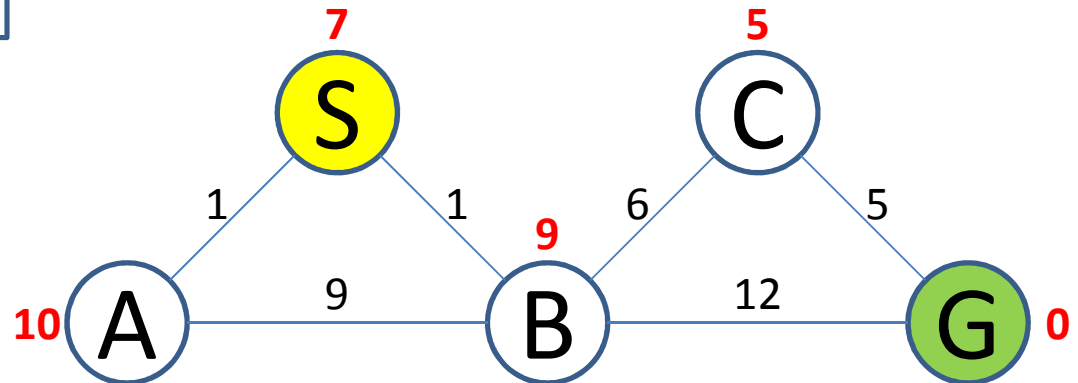
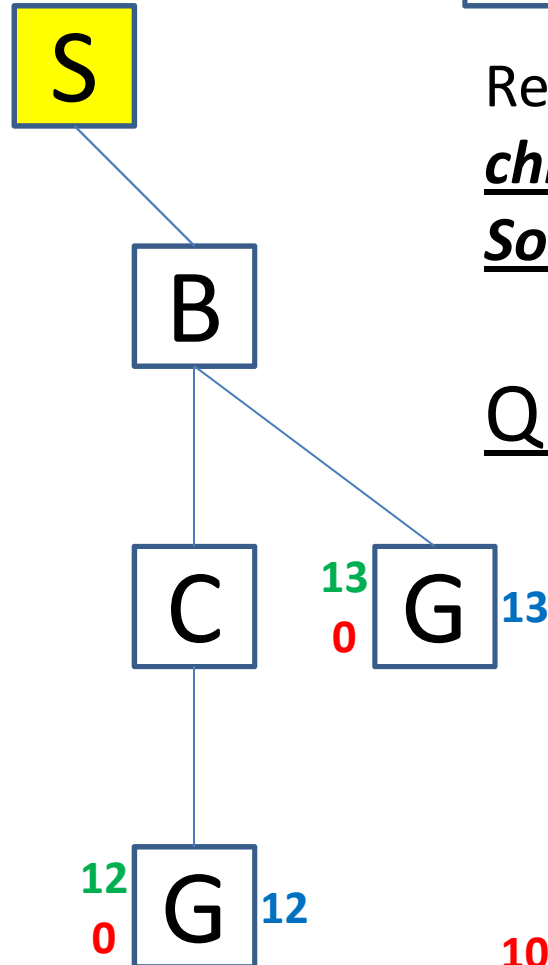


# A\* algorithm by Example

$f = \text{accumulated path cost} + \text{heuristic}$

Remove first path, Create paths to all children, Reject loops and Add paths.  
Sort QUEUE by f

QUEUE: <SBCG, SBG>

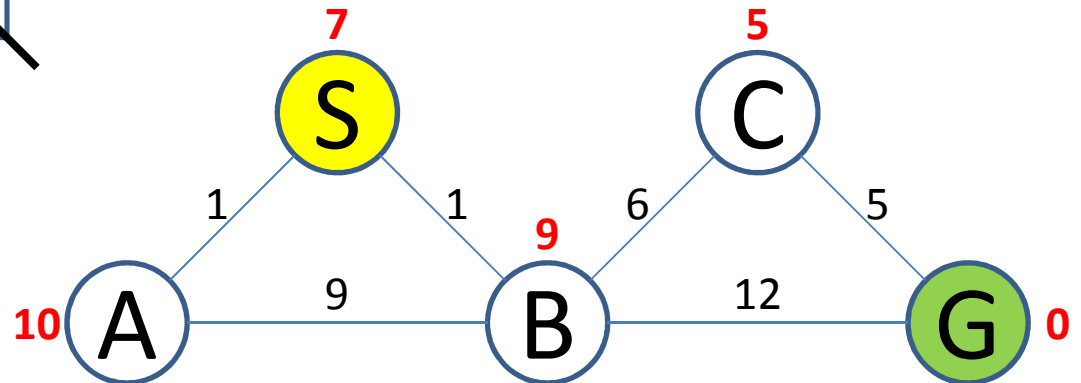
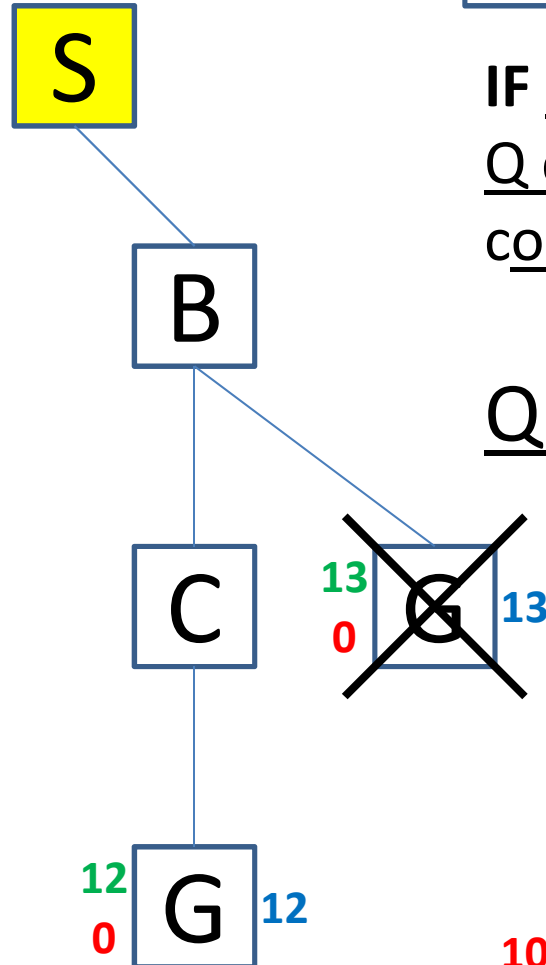


# A\* algorithm by Example

$f = \text{accumulated path cost} + \text{heuristic}$

IF  $P$  terminating in  $I$  with cost  $P$  &&  
 $Q$  containing  $I$  with cost  $Q$  **AND**  
 $\text{cost } P \geq \text{cost } Q$  **THEN** remove  $P$

QUEUE:  $\langle \text{SBCG}, \underline{\text{SBG}} \rangle$

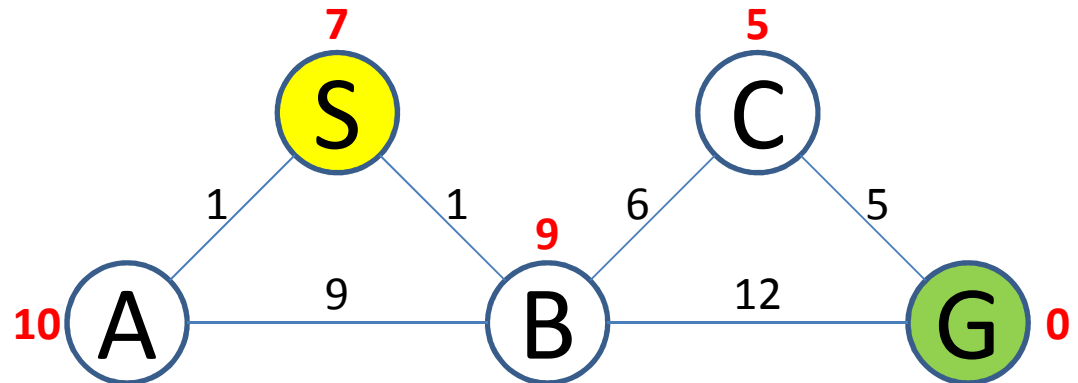
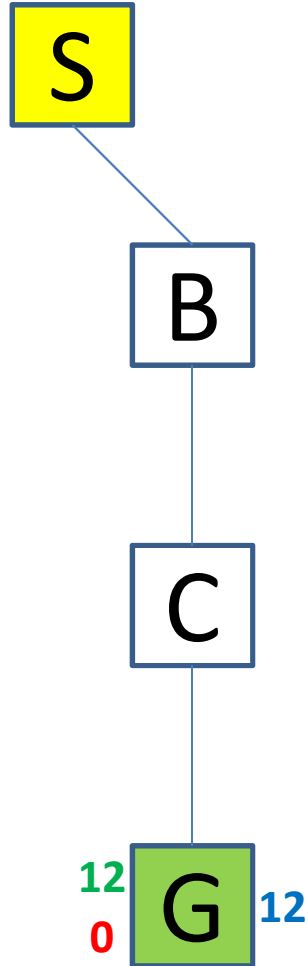


# A\* algorithm by Example

$f = \text{accumulated path cost} + \text{heuristic}$

SUCCESS

QUEUE: <SBCG>

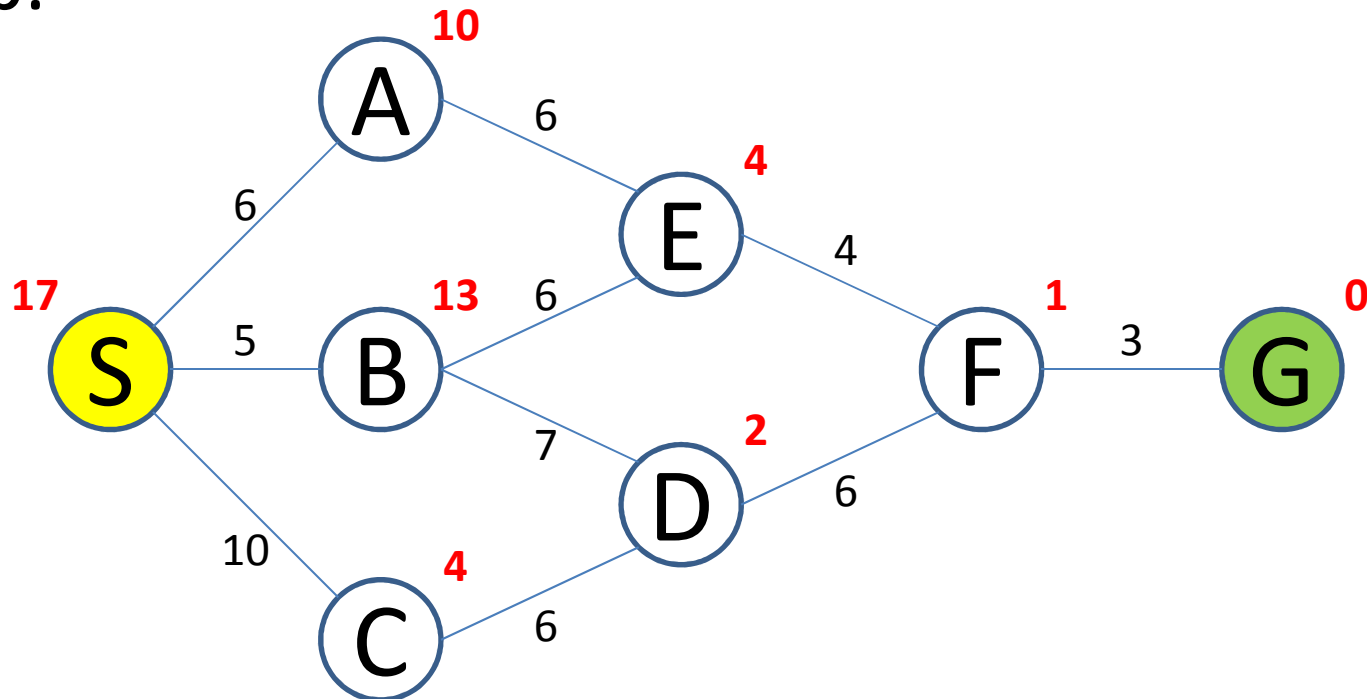


A\*

**PROBLEM**

# Problem

- Perform the  $A^*$  Algorithm on the following figure. Explicitly write down the queue at each step.

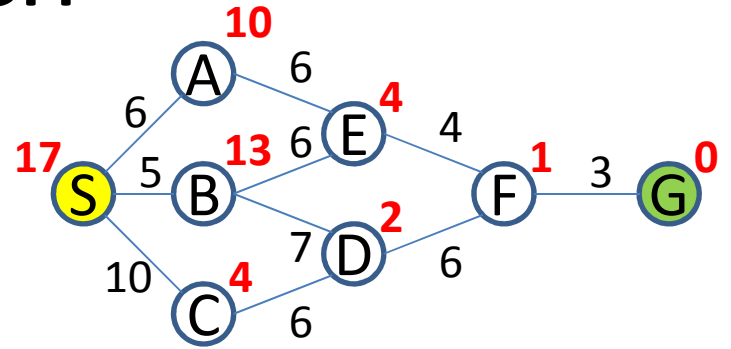


A\*

**A\* SEARCH**



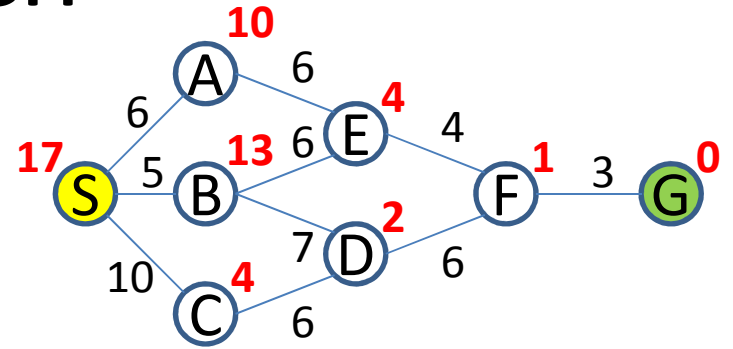
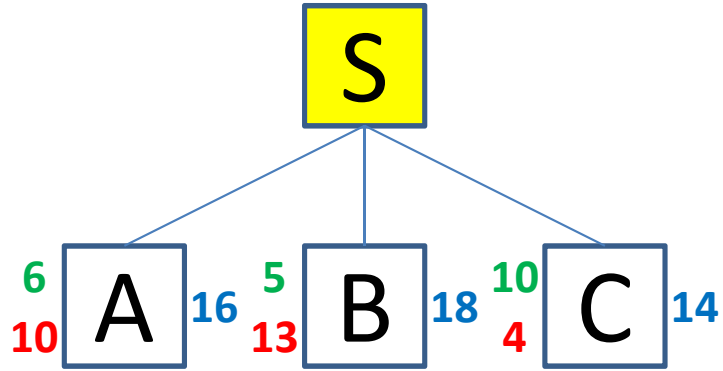
# A\* Search



QUEUE:

S

# A\* Search



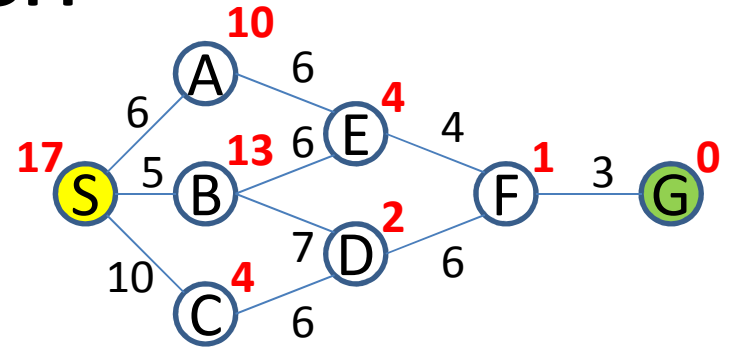
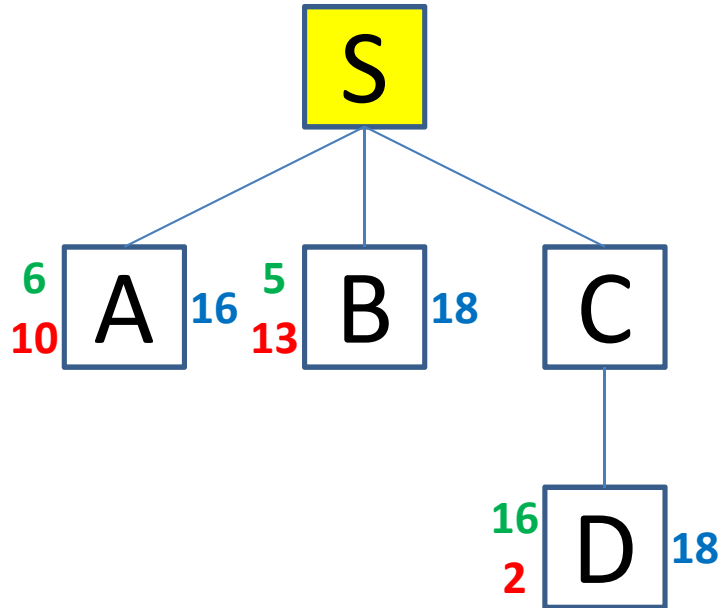
QUEUE:

SC

SA

SB

# A\* Search



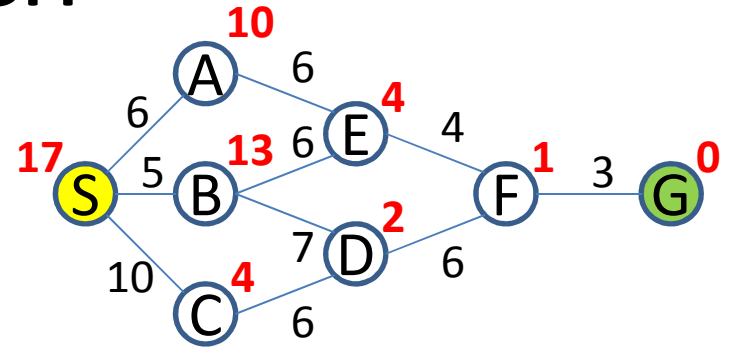
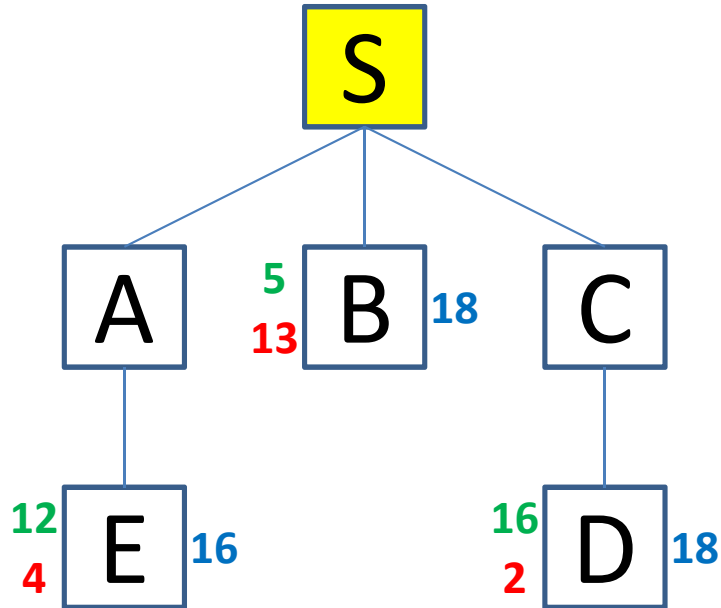
QUEUE:

SA

SCD

SB

# A\* Search



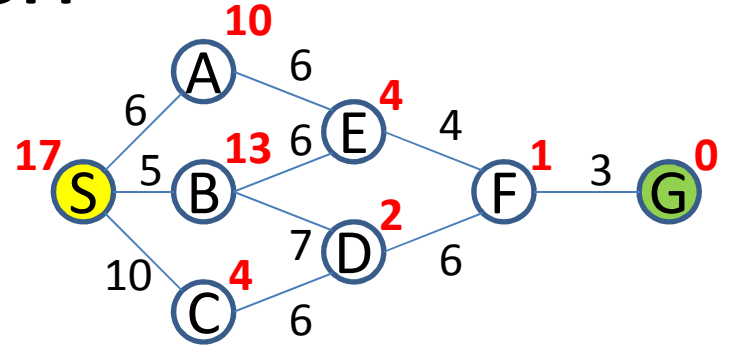
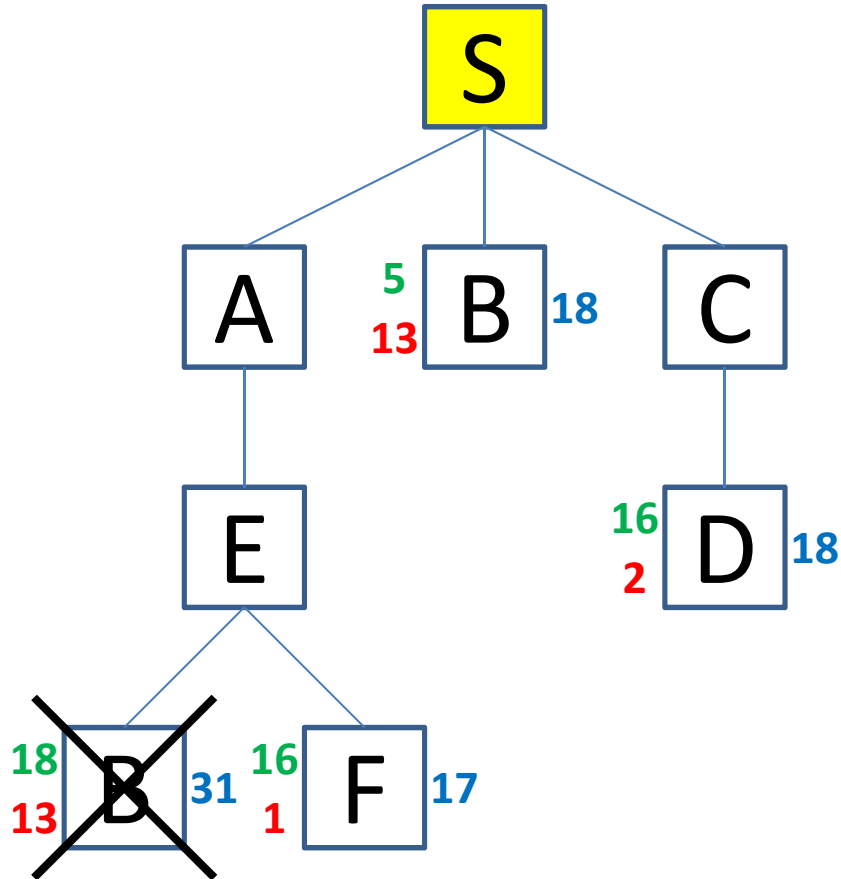
QUEUE:

SAE

SCD

SB

# A\* Search



QUEUE:

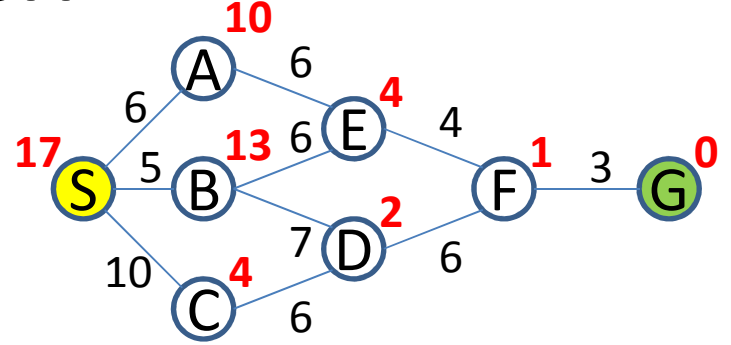
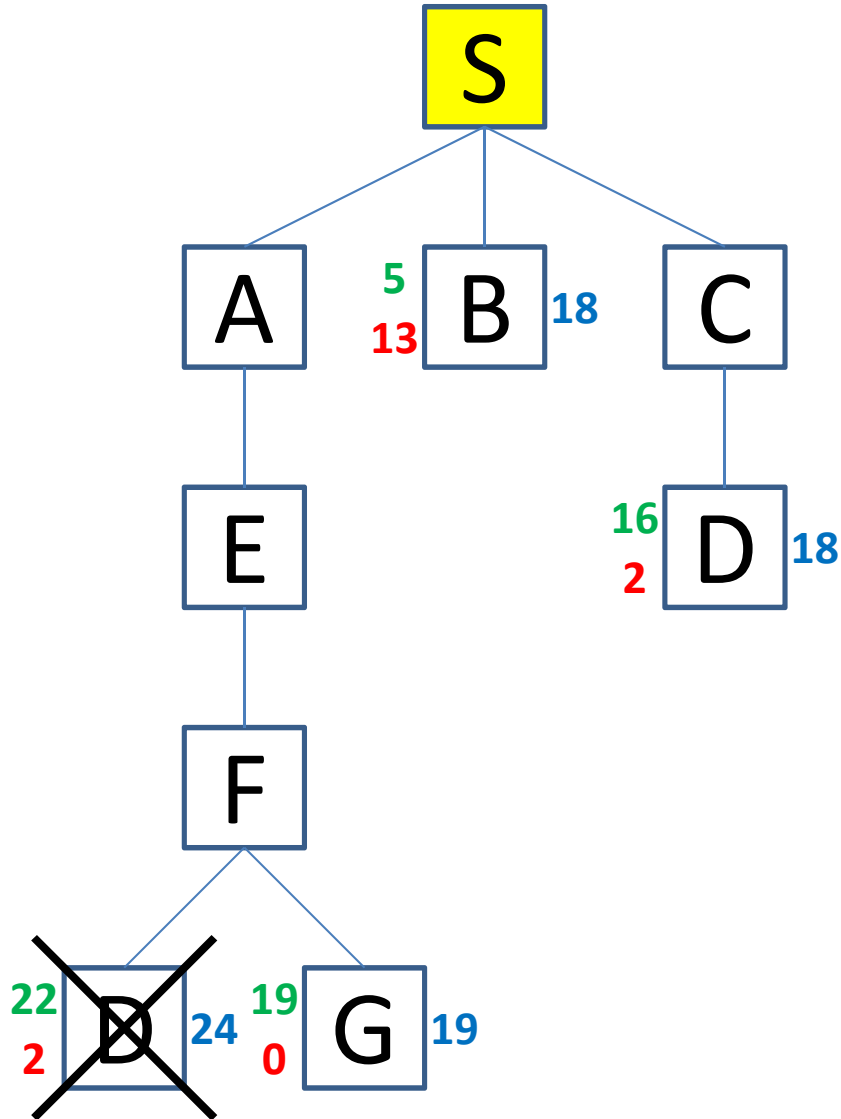
SAEF

SCD

SB

SAEB

# A\* Search



QUEUE:

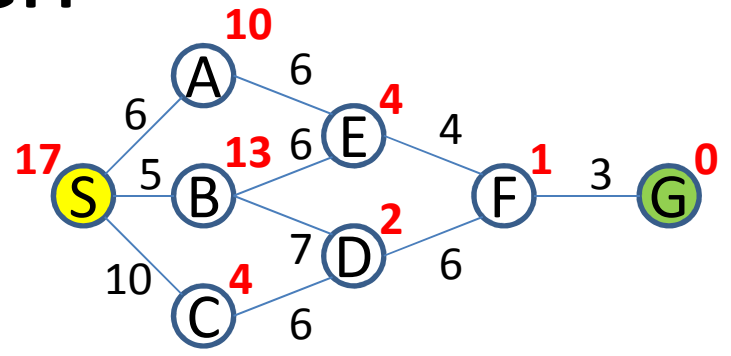
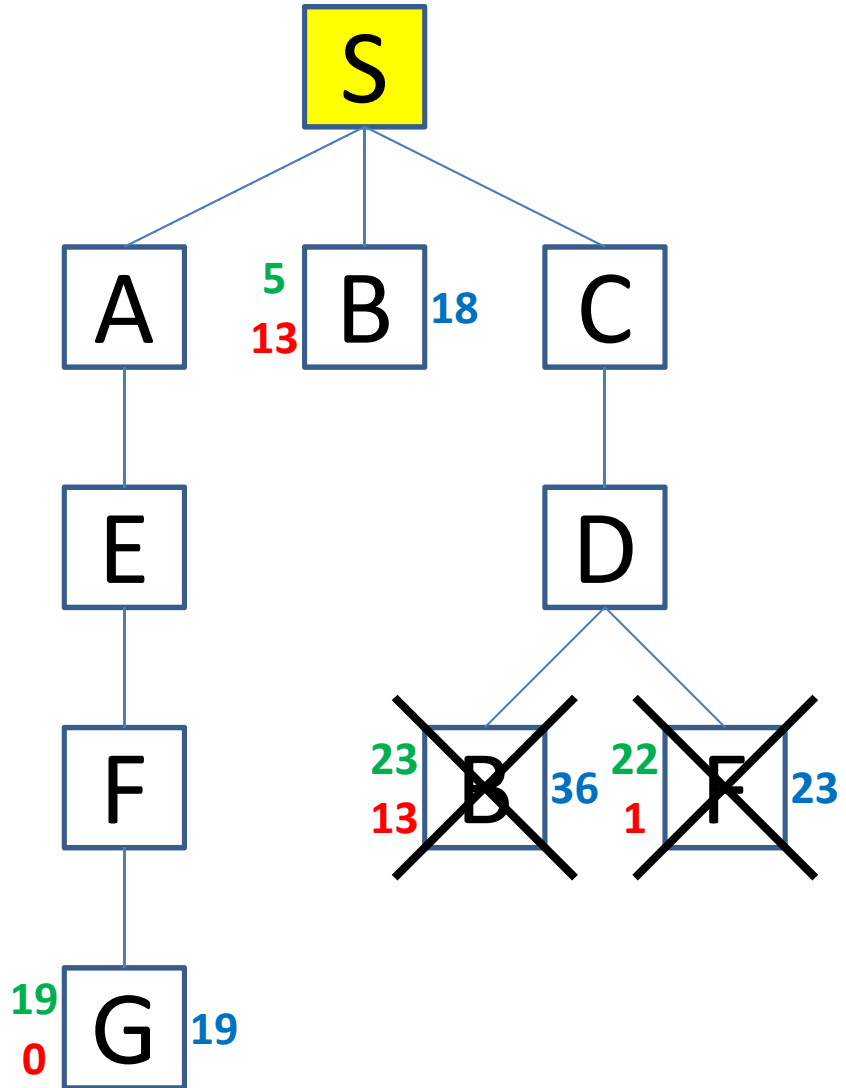
SCD

SB

SAEFG

SAEFD

# A\* Search



QUEUE:

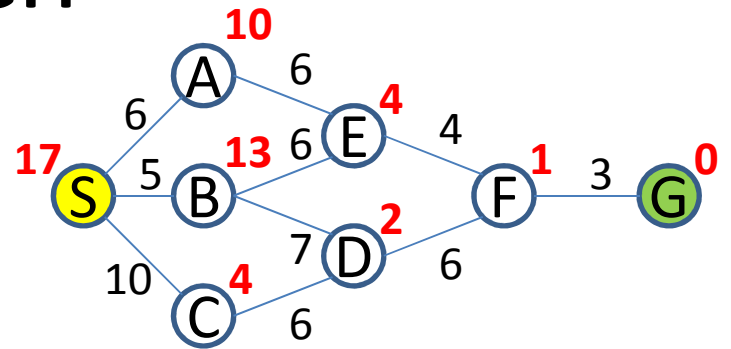
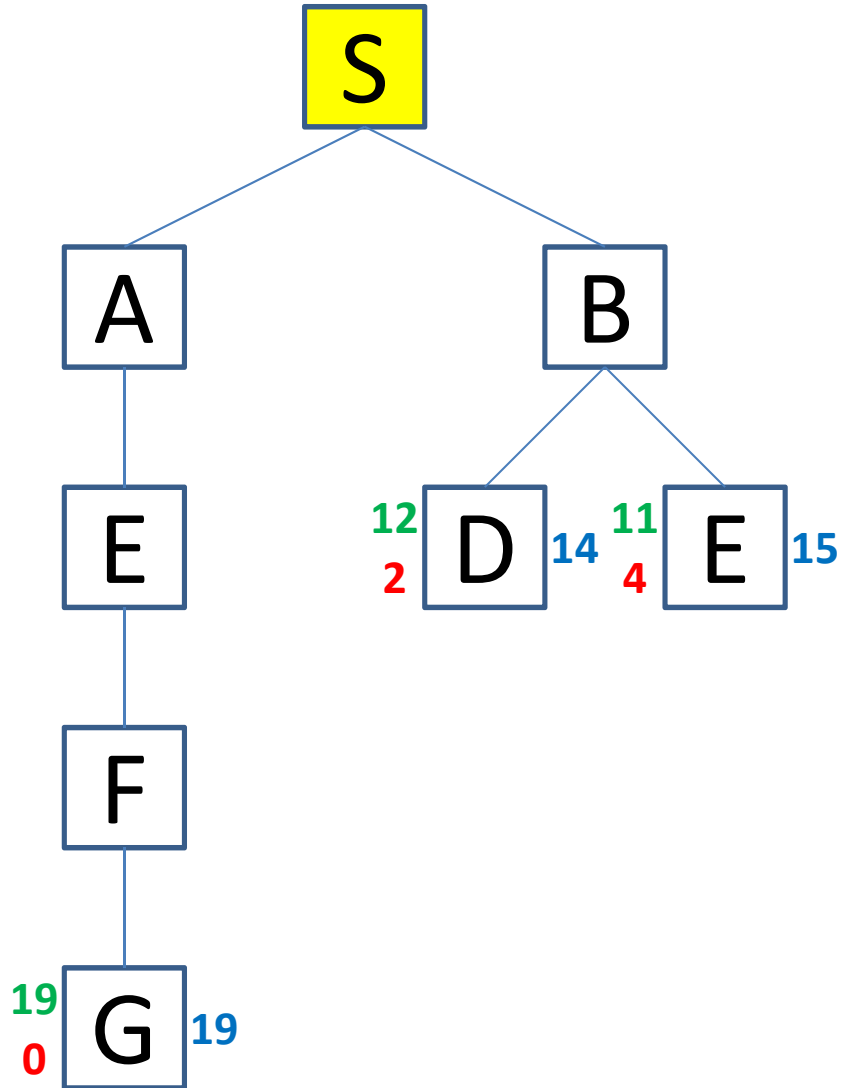
SB

SAEFG

SCDF

SCDB

# A\* Search



QUEUE:

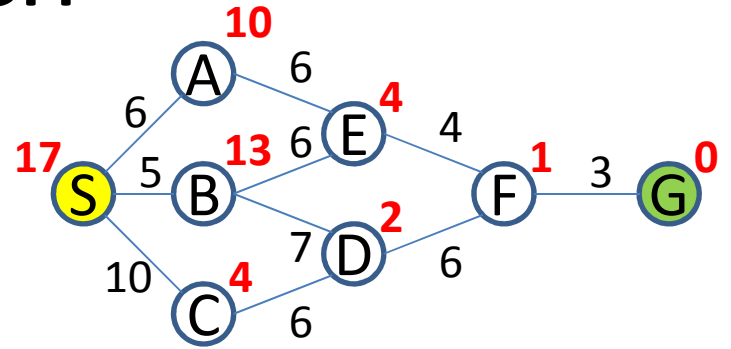
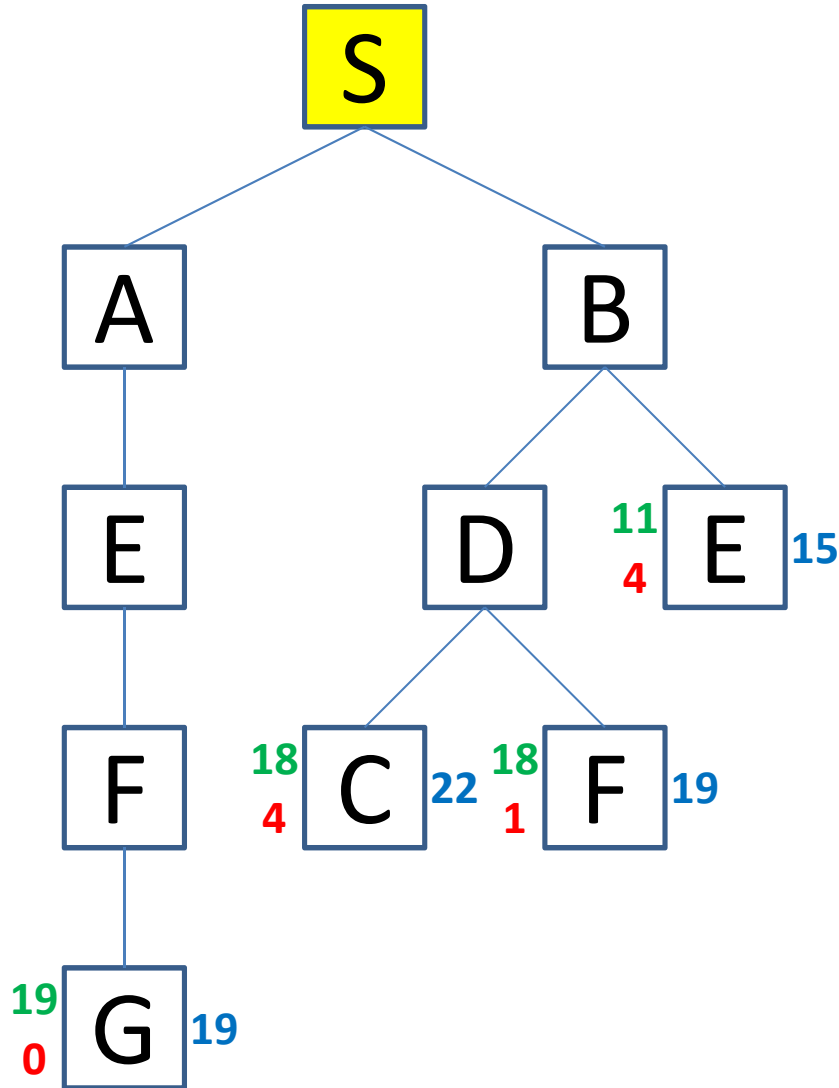
SBD

SBE

SAEFG



# A\* Search



QUEUE:

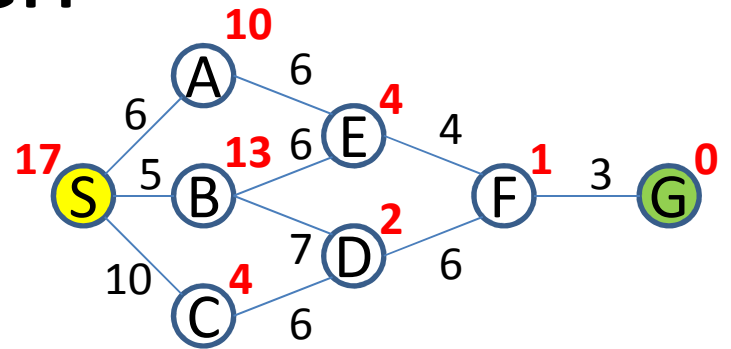
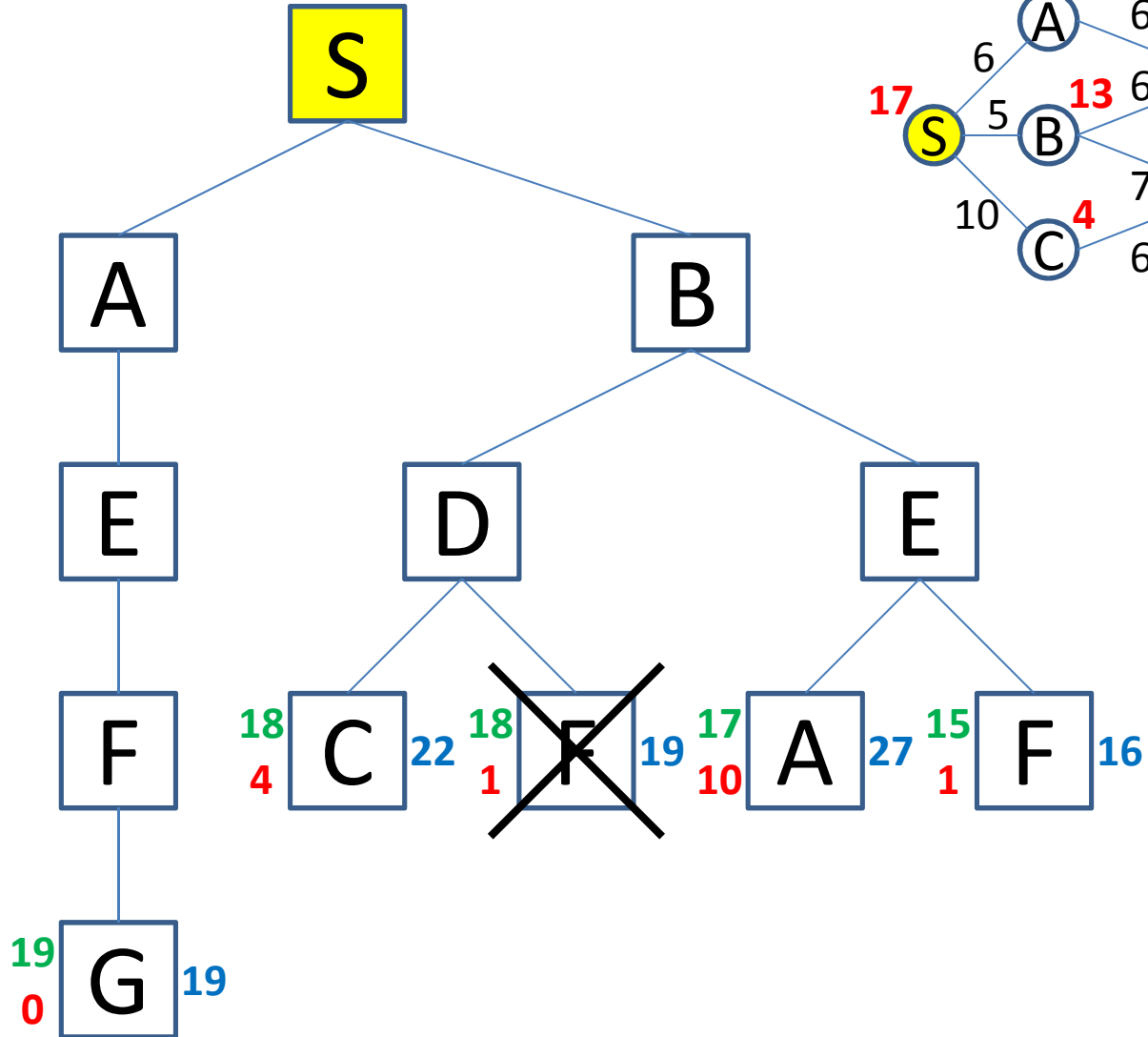
SBE

SBDF

SAEFG

SBDC

# A\* Search



QUEUE:

SBEF

SAEFG

**SBDF**

SBDC

SBEA

# A\* Search

